A search for neutrinoless double-beta decay in tellurium-130 with CUORE

Jeremy Stein Cushman **Dissertation Defense** December 15, 2017





- History and background
- CUORE detector and cryostat
- Detector calibration system
- First physics results

Outline





The early days



- **Becquerel** discovers that uranium randomly \bullet emits lots of particles. Curie & Curie investigate and coin the term "radioactivity."
- **Rutherford** notices that there are two types of emissions, one of which penetrates matter much better than the other; he calls them "alpha" and "beta" particles
- **Becquerel** measures the mass-to-charge ratio of the beta particles, and it exactly matches that of the electron (discovered only 3 years earlier)

- **Soddy & Fajans** establish that beta decay transforms an element into the one to the right of it in the periodic table
- Everyone thinks that beta particles should have specific energies, but Meitner & Hahn show that beta particles are actually emitted in an energy continuum
- **Nearly Everyone:** Is the law of conservation of energy in trouble?







The early days



- After 20 years of debate, **Pauli** proposes the idea • **Majorana** proposes that the neutrino and of the neutrino to conserve energy and antineutrino may be the same particle; this would not have a noticeable effect on beta decay momentum in beta decays
- Fermi creates a formal theory of beta decay incorporating the neutrino
- Goeppert-Mayer postulates double beta decay: if particles can decay by emitting an electron and a neutrino, they should also be able to emit 2 electrons and 2 neutrinos

Furry postulates that if neutrinos are their own • antiparticles, then atoms should be able to decay by emitting just 2 electrons and no neutrinos



Double beta decays

Ordinary $(2\nu\beta\beta)$ Observed in several isotopes



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Neutrinoless ($0\nu\beta\beta$) Hypothesized, if neutrinos are Majorana fermions







- Double beta decay is a second-order process (highly suppressed)
- We have no chance of seeing it directly in isotopes for which single beta decay is allowed
- We need to look for cases where double beta decay is allowed and single beta decay is forbidden



129.903508 u



Detecting 0vBB decay

Goal: Measure the summed energy of both electrons released in the decay

Ordinary $(2\nu\beta\beta)$: Some energy goes into electrons. Some energy escapes with neutrinos.

Neutrinoless $(0\nu\beta\beta)$:

Summed energy of electrons is always equal to *Q*-value. No energy escapes.

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Observation of $0\nu\beta\beta$ decay would be the first evidence of lepton number violation and unambiguously establish the Majorana nature of the neutrino



- Most measured half-lives for $2\nu\beta\beta$ decay are on the order of 10^{21} years
 - Compare to lifetime of the universe: 10¹⁰ years
 - Compare to Avogadro's number: 6 × 10²³
 - A mole of the isotope will produce ~1 decay/day
- If it exists, the half-lives of $0\nu\beta\beta$ decay would be much longer
 - ¹³⁰Te $0\nu\beta\beta$ decay limit is > 10²⁴ years
 - A mole of ¹³⁰Te produces < 1 neutrinoless decay/year
 - A half-life of 10²⁶ years requires 32 kg of ¹³⁰Te to see 1 decay/year





ander avoguet



Half-lives

$$(T_{1/2}^{0\nu})^{-1} = G^{0\nu}(Q,Z) |M^{0\nu}|^2 \frac{|\langle m_{\beta\beta} \rangle}{m_e^2}$$
$$T_{1/2}^{0\nu} = 0\nu\beta\beta \text{ half-life}$$
$$G^{0\nu}(Q,Z) = \text{phase space factor } (\propto Q^5)$$
$$M^{0\nu} = \text{nuclear matrix element}$$
$$\langle m_{\beta\beta} \rangle = \text{effective } \beta\beta \text{ neutrino mass}$$
$$m_e = \text{electron mass}$$

- Shorter half-lives are easier to measure, so choose an isotope with a high **phase space factor** (high *Q*-value) and high nuclear matrix element
- Nuclear matrix element is calculated theoretically, with different models differing by factors of ~2
- Effective Majorana neutrino mass gives hints about absolute neutrino mass



Neutrino masses



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Single beta decay

$$m_{\beta} = \sqrt{\sum_{i} |U_{ei}|^2 m_i^2}$$

Double beta decay

$$m_{\beta\beta} = \left| \sum_{i} U_{ei} m_i \right|$$

• Calculated assuming model of light Majorana neutrino exchange

 Requires theoretical models of nucleus (nuclear matrix elements) and assumptions on value of axialvector coupling constant g_A



- Choose a source with a high **isotopic abundance** of the 0νββ decay emitter
- Create a detector with a high **detection** efficiency and good energy resolution in a **low-background** environment
- Run experiment for a long exposure time with a large **total mass** of the source isotope

$T_{1/2}^{0\nu}$ sensitivity $\propto a \cdot \epsilon \sqrt{\frac{M \cdot t}{h \cdot \delta E}}$ a = source isotopic abundance ϵ = detection efficiency M = total masst = exposure time $b = background rate at 0 \nu \beta \beta energy$ δE = energy resolution



0vBB decay detection techniques

130Te

- Bolometer-based searches: Cuoricino/CUORE-0/CUORE
- Loaded organic scintillator: SNO+
- $T_{1/2} > 4.0 \times 10^{24}$ y with CUORE-0





76 Ge

- High-purity germanium detectors: GERDA/ MAJORANA
- $T_{1/2} > 5.3 \times 10^{25} \text{ y}$

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136 Xe

- Xe scintillation: KamLAND-Zen
- Liquid TPC & scintillation: EXO-200, nEXO
- Gas TPC: NEXT-100, PandaX-III
- $T_{1/2} > 1.1 \times 10^{26} \text{ y}$



NEMO-3/ SuperNEMO

- Source foils with tracking and calorimetry
- Half-lives for ⁴⁸Ca, ⁸²Se, 96 Zr, 100 Mo, ...



A world of experiments



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Recent results:

Experiment	Isotope	Detector technology	Half-life limit	Iso. exposure
GERDA	$^{76}\mathrm{Ge}$	Ionization	$> 5.3 \times 10^{25} \text{ yr}$	$34 \text{ kg} \cdot \text{yr}$
NEMO-3	$^{100}\mathrm{Mo}$	Tracker, calorimeter	$> 1.1 \times 10^{24} \text{ yr}$	$35 \mathrm{kg} \cdot \mathrm{yr}$
CUORE-0	$^{130}\mathrm{Te}$	Bolometers	$> 4.0 \times 10^{24} \text{ yr}$	$30 \mathrm{kg} \cdot \mathrm{yr}$
EXO-200	136 Xe	Liquid TPC	$> 1.1 \times 10^{25} \text{ yr}$	$100 \mathrm{kg} \cdot \mathrm{yr}$
KamLAND-Zen	136 Xe	Scintillation	$> 1.1 \times 10^{26} \text{ yr}$	$504 \mathrm{kg} \cdot \mathrm{yr}$

Current and future experiments:

Experiment	Isotope	Detector technology	Sensitivity	Iso. mass	Start
GERDA (Phase II)	⁷⁶ Ge	Ionization	$1 \times 10^{26} \text{ yr}$	30 kg	2016
MAJORANA DEMO.	$^{76}\mathrm{Ge}$	Ionization	$2 \times 10^{26} \text{ yr}$	26 kg	2016
SuperNEMO	82 Se	Tracker, calorimeter	$1 \times 10^{26} \text{ yr}$	100 kg	2020?
CUORE	$^{130}\mathrm{Te}$	Bolometers	$9 \times 10^{25} \text{ yr}$	206 kg	2017
SNO+	$^{130}\mathrm{Te}$	Scintillation	$9 \times 10^{25} \text{ yr}$	800 kg	2018?
EXO-200 (Phase II)	136 Xe	Liquid TPC	$6 \times 10^{25} \text{ yr}$	76 kg	2016
NEXT-100	136 Xe	Gas TPC	$6 \times 10^{25} \text{ yr}$	90 kg	2018?
PandaX-III	136 Xe	Gas TPC	$1 \times 10^{26} \text{ yr}$	180 kg	2019?
KamLAND-Zen	¹³⁶ Xe	Scintillation	$2 \times 10^{26} \text{ yr}$	$600 \mathrm{kg}$	2016

Present and future



Advantages of CUORE

- ¹³⁰Te: High natural abundance (no enrichment required), good Q-value (above Compton edge of 2615 keV line), relatively accessible 0vββ decay half-life



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• Excellent energy resolution of TeO₂ bolometers (~0.2% FWHM resolution at 2615 keV)

$$\mathcal{O}_{\nu}(Q,Z)|M^{0\nu}|^2 \frac{|\langle m_{\beta\beta}\rangle|^2}{m_e^2}$$





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Outline









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CUORE





- The Cryogenic Underground Observatory for Rare Events (CUORE) searches for $0\nu\beta\beta$ decay in ¹³⁰Te
- Located deep underground at the Laboratori Nazionali del Gran Sasso (LNGS) in Assergi, Italy
- Composed of 988 TeO₂ crystals (total mass of 742 kg, with 206 kg of ¹³⁰Te)
- 19 times the mass of the predecessor experiment CUORE-0
- Runs in a new custom-built cryostat with much lower backgrounds than CUORE-0

CUORE











Phys. Rev. Lett. **115**, 102502 (2015)

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 $T_{1/2}^{0\nu\beta\beta} > 4.0 \times 10^{24} \text{ y (90\% C.L.)}$

Projected: $T_{1/2}^{0\nu\beta\beta} > 9 \ge 10^{25} \text{ yr (90\% C.L.)}$ $m_{\beta\beta} < 50 - 130 \text{ meV}$



Bolometric detection

- Bolometers are operated at ~15 mK, so that single particle energy deposits cause a measurable spike in temperature
- Temperature is measured by measuring voltage across temperature-dependent resistors (thermistors)





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• Each TeO₂ bolometer crystal is instrumented with a resistive heater and a neutron transmutation doped germanium (NTD-Ge) thermistor





Cryostat and shielding



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- Bolometers are assembled into towers and cooled by pulse-tubeassisted dilution refrigerator
- Detector towers are surrounded by copper and lead shields at successively colder temperatures
- Cryostat is surrounded by large lead shield and borated polyethylene neutron shield
- Side lead and bottom lead shields are ancient Roman lead



Ancient Roman lead





- Radioactive shielding can harm experiment as much as it helps
- All lead contains radioactive ²¹⁰Pb from the ²³⁸U decay chain $(^{210}Pb half-life = 22 years)$ when mined
- Ancient Roman lead recovered from shipwreck is used for CUORE ullethttp://www.nature.com/news/2010/100415/full/news.2010.186.html

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Projected backgrounds



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Building the detector towers





Building and commissioning the cryostat







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Installing the detectors

Wiring and electronics



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Outline





Calibration

- Voltage signals from the thermistors must be calibrated to determine the energy of each event
- CUORE only measures energy, so precise energy calibration is crucial



- A two-step calibration process is used:
 - 1. The thermistor gain is stabilized over time
 - 2. Thermistor readings are calibrated to absolute energies

Pulse max



Baseline



Calibration hardware

- Bolometers require independent *in situ* energy calibration
 - Bolometers must be calibrated at their operating temperature
 - Moving sources into position must not affect bolometer temperature
- We need to preserve ultraclean conditions for physics data taking

 - Calibration sources must be visible to detectors only during calibration • Background contribution of calibration hardware must be low

• Procedure must be stable over expected 5-year lifetime of the experiment



Calibration hardware



- Only one tower
- Sources can be placed outside cryostat but inside shielding
- Sources can be positioned by hand

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CUORE



- Outer towers shield inner towers
- Sources must be cold and placed among towers inside cryostat
- Source deployment must be automated
- J. S. Cushman *et al*. NIM A **844**, 32-44 (2017)



Calibration strings

- - Twelve source strings are lowered into the cryostat during calibration periods
 - Cooled from 300 K to the bolometer operating temperature of ~15 mK

Each source string contains:

- 25 or 26 source capsules of thoriated tungsten wire (containing ²³²Th)
- 8 weight capsules
- 1 PTFE guide ball







Sources produced at UW-Madison and Yale



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String production









Calibration source deployment



Strings are lowered under their own weight through a series of guide tubes

6 inner source strings

- 3.5 Bq each
- Guided between the bolometer towers to illuminate the inner detectors

6 outer source strings

- 19.4 Bq each
- Guided to outside of 50 mK vessel to illuminate outer detectors

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4-K Thermalization



• Source capsules are fully thermalized at 4 K before being lowered further into the cryostat



• 4 K stage is cooled by pulse tube cryocoolers and thus has significant cooling power





- Staggered deployment of all 12 strings takes about 24 hours



Cryostat temperature

• Deployment of a single inner string takes about 6 hours


Integration







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• All system control and readout is done through a rack near the cryostat



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Control electronics

• Signal and power cables connect the rack to the motion hardware on the cryostat





- Majority of the motion control electronics are contained inside 4 boxes
- 3 strings + 4-K thermalizer controlled by each box
- Contain power supplies, motor controllers, custom PCBs, relays, and more
- All designed, built, and tested at Yale and installed at LNGS



Software control

- Wrote software that controls and monitors every aspect of the calibration system during operation
- Allows for full, automated, and remote operation of the calibration system



- Clear visual overview allows operator to see • current status and next steps
- Monitors string position, string tension, guide tube temperatures, vacuum pressure, and other parameters during deployments to ensure safe operation
- Saves and records all parameters for future • review and analysis
- Successfully used in first deployments of calibration sources for CUORE





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Data processing overview





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Acquiring data

- 984/988 (99.6%) of detectors are operational; 90% are used in this analysis
- We acquire data continuously from operating detectors at a rate of 1 kHz
- We trigger on a channel and save a 10-second waveform when the slope of the signal is above a channel-dependent threshold



- Acquired in runs (~1 day) and grouped into datasets (~1 month), which begin and end with a calibration
- We compute an average pulse shape and average noise power spectrum for each channel and use this to filter the waveforms





Thermal gain stabilization

- Heat capacity of the TeO₂ crystals (C∝T³) and resistance of the NTD Ge thermistors are strongly temperature dependent
- Therefore, our pulse amplitude for a given energy deposition is strongly dependent on temperature (which fluctuates slightly while taking data)
- To correct for this, we periodically (every ~300 s) inject fixed amounts of energy with Si heaters attached to the crystals



Thermal gain stabilization

- Baseline voltage of the pulse is an (uncalibrated) measure of bolometer temperature
- Fit a curve to determine the estimated heater pulse amplitude at any baseline



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• Each event is assigned an arbitrary-unit stabilized amplitude:

Pulse stabilized amplitude	Pulse raw amplitude
5000	- Heater amplitude at pulse baselir





Monthly calibration

- We still need to convert stabilized amplitudes to real-world energies
- After deploying the ²³²Th sources, we acquire several days of calibration data
- Provides several strong peaks in the energy spectrum



• We use these lines to create a channel-by-channel map from stabilized amplitude to true energy



- In order to select candidate $0\nu\beta\beta$ decay events, we apply a variety of cuts to the data
- Several pulse shape parameters are measured, and limits are set on:
 - Baseline slope
 - Rise time and shape
 - Decay time and shape



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Event selection

- We also only accept events that are not simultaneous with events in other crystals
 - Gammas often Compton scatter in multiple crystals
 - Muons almost always deposit energy in multiple crystals





Physics spectrum

- Calibrated physics spectrum from our first two datasets, after event selection
- 83.6 kg yr of TeO₂ exposure, from Dataset 1 (May June) and Dataset 2 (August September)
- Factor of 4 reduction in background rate in 0vββ decay region of interest compared to CUORE-0, thanks to new cryostat





Selection efficiency

- We need to evaluate the overall selection efficiency: probability of us observing a $0\nu\beta\beta$ decay event given that one has occurred
 - Evaluate efficiency on gamma lines in the physics spectrum (from ⁴⁰K and ²⁰⁸Tl)
 - Overall, our efficiency on gamma lines is $(90.5 \pm 1.9)\%$ in Dataset 1 and $(92.7 \pm 1.4)\%$ in Dataset 2
- $0\nu\beta\beta$ decay events are entirely contained in 1 crystal 88.3% of the time (estimated from simulation)
- Together, we estimate that we would see $(79.9 \pm 1.9)\%$ of $0\nu\beta\beta$ decays in Dataset 1 and $(81.9 \pm 1.4)\%$ in Dataset 2

Selection efficiency ($\overset{\circ}{,}$				
Dataset 1	Dataset			
97.6 ± 1.1	96.7 ± 1			
93.9 ± 1.6	96.8 ± 1			
99.8 ± 0.1	$100.\pm0$			
99.0 ± 0.1	99.0 ± 0			
90.5 ± 1.9	92.7 ± 1			
88.3 ± 0.1	88.3 ± 0			
	Selection ef Dataset 1 97.6 ± 1.1 93.9 ± 1.6 99.8 ± 0.1 99.0 ± 0.1 90.5 ± 1.9 88.3 ± 0.1			



Line shape

- We need to know what a $0\nu\beta\beta$ decay signal might look like
- For this, we use the 2615 keV calibration line
 - Close in energy to $Q_{\beta\beta} = 2528 \text{ keV}$
 - Sufficient channel-by-channel statistics to estimate line shape



- (a) Main photopeak (modeled as sum of 3 Gaussians)
- (b) Compton multi-scatter continuum
- (c) X-ray escape after 2615 keV deposition
- (d) Flat background
- (e) Coincident 2615 keV and 583 keV deposition followed by pair production and single escape



Calibration resolution

- We use the 2615 keV line to estimate our calibration resolution
- Physics-exposure-weighted harmonic mean resolution = 8.3 keV (in calibration data at 2615 keV)





Full spectrum analysis

- lines in the physics spectrum



• Using the 2615 keV calibration line shape, we perform fits to other visible

• Allows us to estimate our resolution and energy bias in the physics data

Resolution and energy bias



- Extrapolating to $Q_{\beta\beta} = 2528$ keV, we find a physics resolution of:
 - (8.2 ± 0.4) keV in Dataset 1
 - (7.1 ± 0.7) keV in Dataset 2
- Working hard to achieve resolution goal of 5.0 keV



• We see no evidence of an energy bias, and conservatively set a systematic uncertainty of ± 0.5 keV on $Q_{\beta\beta}$



Blinded spectrum

- The spectrum is blinded during data analysis by inserting a fake peak at $Q_{\beta\beta}$
- Events are swapped between the region around $Q_{\beta\beta}$ and 2615 keV



CUORE physics spectrum (blinded)



Blinded spectrum

- The spectrum is blinded during data analysis by inserting a fake peak at $Q_{\beta\beta}$ • Events are swapped between the region around $Q_{\beta\beta}$ and 2615 keV





- Unbinned extended maximum likelihood fit in the region of interest
- Using the line shapes in each channel obtained from calibration data
- Floating parameters: 0vββ decay rate, background rate, ⁶⁰Co location, and ⁶⁰Co rate



Region of interest

Best-fit decay rate: $(-1.0 \ ^{+0.4}_{-0.3} \ (\text{stat.})) \times 10^{-25} \ \text{yr}^{-1}$

Background index (no-signal model): (0.014 ± 0.002) counts/(keV kg yr)



• We account for several systematic uncertainties:

- Line shape (perhaps the $0\nu\beta\beta$ decay peak does not have the 3-Gaussian structure)
- Resolution (there is uncertainty in the resolution evaluation due to low background statistics)
- negative log-likelihood curve appropriately

	Absolute uncertainty $[vr^{-25}]$	Relative unce
Recolution		1 5
		1.5
Energy reconstruction		0.2
Line shape	0.02	2.4
Background shape	0.05	0.8
Efficiency		1.8

Systematic uncertainties

- Efficiency (there is uncertainty in our efficiency for the same reason)
- Background shape (it could be slightly not flat)

• For each, we evaluate an absolute and relative bias using Monte Carlo simulations and adjust the





Half-life limit

to obtain a 90%-C.L. limit on 0vββ decay



Strongest limit on 0vββ decay in ¹³⁰Te to date

• Integrate the negative log-likelihood in the physical region (decay rate > 0)



Sensitivity

limit given the background rate we observe



• We perform 20,000 toy Monte Carlo experiments to evaluate median half-life

- Sensitivity of our search (dashed red line): $7.5 \times 10^{24} \text{ y}$
- Probability of observing a more stringent limit than the one we observe (solid red line): 2.6%



Effective Majorana mass

- - $0\nu\beta\beta$ decay is mediated by light neutrino exchange
 - $g_A = 1.27$ (free space value)
- We obtain $m_{\beta\beta} < 140 390$ meV (depending on nuclear matrix elements)



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• We can interpret these results as an effective Majorana neutrino mass assuming:

•Nucl. Phys. A 818, 139 (2009)

• Phys. Rev. Lett. 105, 252503 (2010)

Half-life limits:

- ¹³⁰Te: 1.5×10^{25} yr from this analysis
- •⁷⁶Ge: 5.3 × 10²⁵ yr from Nature 544, 47–52
- •¹³⁶Xe: 1.1 × 10²⁶ yr from Phys. Rev. Lett. 117, 082503 (2016)
- ¹⁰⁰Mo: 1.1 × 10²⁴ yr from Phys. Rev. D 89, 111101 (2014)
- CUORE sensitivity: 9.0×10^{25} yr

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- We have collected almost 100 kg yr of exposure with CUORE
- CUORE has set a world-leading limit on ¹³⁰Te $0\nu\beta\beta$ decay, greater than 10²⁵ years: arXiv:1710.07988
- The CUORE cryostat, a huge engineering feat, has been operating smoothly and reliably in these first datasets



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Summary

- With 5 years of live time, the sensitivity of CUORE will improve by over an order of magnitude from its current value
- Thanks to the DOE Office of Science, Nuclear Physics, and Yale University for funding this research
- More physics results are on the way!





Thanks

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Backup

Cryostat support structure

Calibration integration

Line fitting strategy

- Perform a simultaneous unbinned extended maximum likelihood fit over all channels, with a separate fit for each line in the background spectrum
- Fit parameters:
 - Fixed, and split by channel:

 - Exposure (some channels were not live in some datasets) • Reference width (each channel has a different resolution)
 - Floating, and split into two layers (inner and outer detectors):
 - Peak rate (counts/kg yr)
 - Background rate (counts/keV kg yr)
 - Floating, and common to all channels:
 - Overall scaling of resolution (the resolution is energy-dependent)
 - Peak mean (floating in order to evaluate our energy reconstruction)

Line fit results

Energy	Signal rate	Background rate	FWHM resolution	Bias
[keV]	$[counts/(kg \cdot yr)]$	$[counts/(keV \cdot kg \cdot yr)]$	[keV]	$[\mathrm{keV}]$
961/ 511	2.04 ± 0.33 (inner)	0.011 ± 0.002 (inner)	$8.40 \pm 0.64 \text{ (DS 1)}$	0.02 ± 0.18
2014.011	6.07 ± 0.34 (outer)	0.015 ± 0.002 (outer)	$7.18 \pm 0.43 \text{ (DS 2)}$	0.02 ± 0.10
1/60 822	44.0 ± 1.5 (inner)	0.418 ± 0.073 (inner)	$5.54 \pm 0.13 \text{ (DS 1)}$	0.02 ± 0.07
1400.022	64.1 ± 1.2 (outer)	0.453 ± 0.099 (outer)	$5.58 \pm 0.11 (DS 2)$	-0.02 ± 0.01
1229 /09	14.0 ± 1.0 (inner)	0.561 ± 0.018 (inner)	$5.23 \pm 0.15 \text{ (DS 1)}$	0.12 ± 0.05
1002.432	47.2 ± 1.0 (outer)	0.581 ± 0.022 (outer)	$5.68 \pm 0.16 \text{ (DS 2)}$	-0.12 ± 0.00
1173 998	13.6 ± 1.0 (inner)	0.790 ± 0.022 (inner)	$4.90 \pm 0.18 \text{ (DS 1)}$	-0.08 ± 0.05
1110.220	44.4 ± 1.0 (outer)	0.981 ± 0.037 (outer)	$4.88 \pm 0.14 \text{ (DS 2)}$	-0.00 ± 0.00
011 204	3.64 ± 0.78 (inner)	1.18 ± 0.03 (inner)	$3.74 \pm 0.50 \text{ (DS 1)}$	0.06 ± 0.16
911.204	7.88 ± 0.67 (outer)	1.56 ± 0.03 (outer)	$4.45 \pm 0.51 \text{ (DS 2)}$	0.00 ± 0.10
831 818	4.87 ± 0.87 (inner)	1.29 ± 0.03 (inner)	$4.12 \pm 0.27 \text{ (DS 1)}$	0.19 ± 0.11
094.040	18.3 ± 0.8 (outer)	1.77 ± 0.05 (outer)	$4.68 \pm 0.23 \text{ (DS 2)}$	$0.12 \perp 0.11$

$f(E) = \xi_C \xi_\gamma \varepsilon R_{\beta\beta} \left[\mathcal{N}(\chi_{\beta\beta}\mu, \eta\sigma; E) + \kappa_L \mathcal{N}(\epsilon_L \chi_{\beta\beta}\mu, \eta\sigma; E) + \kappa_R \mathcal{N}(\epsilon_R \chi_{\beta\beta}\mu, \eta\sigma; E) \right]$ $+ \xi_{\gamma} \varepsilon R_{\rm Co} e^{-t/\tau_{\rm Co}} \left[\mathcal{N}(\chi_{\rm Co} \mu, \eta \sigma; E) + \kappa_L \mathcal{N}(\epsilon_L \chi_{\rm Co} \mu, \eta \sigma; E) + \kappa_R \mathcal{N}(\epsilon_R \chi_{\rm Co} \mu, \eta \sigma; E) \right]$ $+\varepsilon b\Delta E.$

 $\hat{R}_{\rm Co} = (0.23 \pm 0.08) \text{ counts}/(\text{kg}\cdot\text{yr})$

$$\Gamma^{0\nu} = R_{\beta\beta} \times \frac{\mathcal{M}_{\text{TeO}_2}}{aN_A} = R_{\beta\beta} \times \frac{159.6 \text{ g m}}{(0.3417)(6.022 \times 10^{-3} \text{ cm})}$$

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ROI fit

 $\hat{R}_{\beta\beta} = (-0.13 \pm 0.04) \text{ counts}/(\text{kg}\cdot\text{yr})$

 $\hat{b}_1 = (0.016 \pm 0.002) \text{ counts}/(\text{keV} \cdot \text{kg} \cdot \text{yr})$

 $\hat{b}_2 = (0.015 \pm 0.002) \text{ counts}/(\text{keV} \cdot \text{kg} \cdot \text{yr}).$

 nol^{-1} $\hat{\Gamma}^{0\nu} = (-0.99^{+0.37}_{-0.27}) \times 10^{-25} \text{ yr}^{-1}$ 10^{23} mol^{-1}

Pulse shape cuts

where $\vec{\mu}$ is the vector of parameter means and S is the covariance matrix.

May					
June					
July					
August					
September	•				

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Run time breakdown

155 ROI pulses

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71

Lineshape Bias

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Systematics

$$\chi_{\text{syst}}^{2} = -2 \left(\text{NLL} - \text{NLL}_{0} \right)$$

$$\chi_{\text{syst}}^{2} = \frac{\Gamma^{0\nu} - \hat{\Gamma}^{0\nu}}{\sigma_{\text{syst}}(\Gamma^{0\nu})}, \qquad \sigma_{\text{syst}}(\Gamma^{0\nu}) = \sum_{i} (\sigma_{i,\text{abs}} + \Gamma^{0\nu}\sigma_{i})$$

$$\frac{1}{\chi_{\text{tot}}^{2}} = \frac{1}{\chi_{\text{stat}}^{2}} + \frac{1}{\chi_{\text{syst}}^{2}}.$$

$$\text{NLL} = -\frac{1}{2}\chi_{\text{tot}}^{2}$$

$$\frac{1}{2} \sum_{\substack{i=0\\j=0\\j=0}}^{40} \int_{j=0}^{40} \int_{j=$$

Models for nuclear matrix elements

- Interacting Shell Model (ISM)
 - Nucleus is a collection of fermions that obey the Pauli • **Exclusion** Principle
 - Basis states are harmonic oscillator states with perturbations
 - Includes all possible shell configurations, sums over a small \bullet number of state energies (computational limitations)
- Quasi-Random Phase Approximation (QRPA)
 - Uses particle–hole pair and quasiparticle dynamics to include a larger number of energy states, but in fewer shell configurations
- Interacting Boson Model (IBM)
 - Considers pairs of protons or neutrons as bosons
 - Useful for even-even nuclei

$$M_{0\nu} = \langle {}^{A}\mathbf{X}; 0_{1}^{+}|H|^{A}\mathbf{Y}; J_{F} \rangle$$
$$M_{0\nu} = g_{A}^{2} \left[M_{GT}^{(0\nu)} - \left(\frac{g_{V}}{g_{A}}\right)^{2} M_{F}^{(0\nu)} + M_{T}^{(0\nu)} \right]$$



Semi-empirical mass formula

 $E_B = a_V A - a_S A^{2/3} - a_C \frac{Z}{-}$

 $\delta(A, Z) = \begin{cases} +\delta_0 & Z, N \text{ even } (A \text{ even}) \\ 0 & A \text{ odd} \\ -\delta_0 & Z, N \text{ odd } (A \text{ even}) \end{cases}$



https://en.wikipedia.org/wiki/File:Liquid_drop_model.svg

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$$\frac{Z(Z-1)}{A^{1/3}} - a_A \frac{(A-2Z)^2}{A} + \delta(A,Z)$$



Neutrino mass

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix} = \begin{bmatrix} 0.82 \\ -0.38 \\ 0.44 \end{bmatrix}$$
$$= \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 \\ 0 & 1 \\ -s_{13}e^{i\delta_{CP}} & 0 \end{bmatrix}$$

Double beta decay

$$m_{\beta\beta} = \left| \sum_{i} U_{ei}^2 m_i \right|$$

Single beta decay

$$m_{\beta} = \sqrt{\sum_{i} |U_{ei}|^2 m_i^2}$$

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